

Signed numbers:

There are three ways in which signed binary numbers may be expressed:

- Signed magnitude (SM)
- One's complement and
- Two's complement.

In an 8-bit word, signed magnitude representation places the absolute value of the number in the 7 bits to the right of the sign bit.

Ex: in **8-bit signed magnitude(SM)**, positive 3 is: 00000011

Negative 3 is: 10000011

Ex: in 8-bit **one's complement**, positive 3 is: 00000011

Negative 3 is: 11111100

Ex: Adding 1 gives us -3 in **two's complement** form: 11111101

Ex: convert using SM method $(01011001)_2 = +(1 * 2^6 + 0 * 2^5 + 1 * 2^4 + 1 * 2^3 + 0 * 2^2 + 0 * 2^1 + 1 * 2^0)$

$$= + (64 + 0 + 16 + 8 + 0 + 0 + 1)$$

$$= (+89)_{10}$$

Ex: convert using SM method $(10011100)_2 = - (0 * 2^6 + 0 * 2^5 + 1 * 2^4 + 1 * 2^3 + 1 * 2^2 + 0 * 2^1 + 0 * 2^0)$

$$= - (0 + 0 + 16 + 8 + 4 + 0 + 0)$$

$$= (-28)_{10}$$

7's and 8's complements in octal :

7's = 7 – each digit

$$8's = 7's + 1$$

EX: 7777
 - 2415

 5362 is 7's comp.
 + 1

 5363 is 8's comp.

EX: Perform $7526_8 - 3142_8$ using 8's comp.:

$$\begin{array}{r} 7777 \\ -3142 \\ \hline 4635 + 1 = 4636 \end{array}$$

1 1
7526
+ 4636

Diagram illustrating the subtraction process for the second column (5 - 6):

- 12 - 8 = 4
- 11 - 8 = 3
- 12 - 8 = 4

1 4364 the result

H.W. Perform the following using 8's complement:

$$545_8 - 14_8 =$$

$$6776_8 - 4337_8 =$$

15's and 16's complements in hexadecimal :

EX: Find 15's and 16's comp. of $(1\text{ F A D})_{16}$

15	15	15	15	
- 1	F	A	D	
E	0	5	2	15's comp.
			← 1 +	
E	0	5	3	16's comp.
			←	

EX: Perform $\text{A B E D} - 1\text{ F A D}$ using 16's comp. :

1 1	
A B E D	
+ E 0 5 3	
1 8 C 4 0	the result

H.W. :Perform the following using 16's complement :

$$\text{F E E D}_{16} - \text{D A F 3}_{16} =$$

ANS: 23FA_{16}

$$9\text{ 8 A E}_{16} - 1\text{ F E E}_{16} =$$