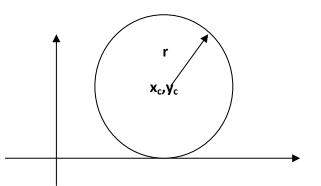
## **Circle Drawing**

The circle is a special kind of curves. The circle is a closed curve with same starting and ending point. Circles are probably the most used curves in elementary graphics.



- A circle is specified by the coordinates of its center (*xc*, *yc*) and its radius (r).
- The circle equation is :  $(x-xc)^2 + (y-yc)^2 = r^2$  ...... (1)
- If the center of the circle is at the origin (0,0) then the equation is :

$$x^2 + y^2 = r^2 \dots (2)$$

Solving equation (1) for y :

$$y=yc\pm\sqrt{r^2-(x-xc)^2}$$

**Note:** To draw a circle increment the x values by one unit from –r to +r and use the above equation to solve for the two y values at each step.

## 1. Direct (implicit) algorithm

In this method the first pixel of circle is at left side as equation

x=xc-r

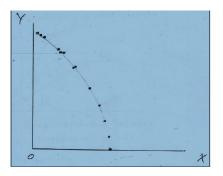
y=yc

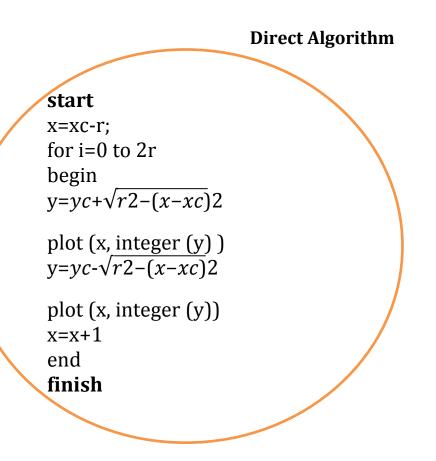
to draw the circle we can increment x from -r to +r or from 0 to 2r by one unit at each step and solving for y

$$y=yc\pm\sqrt{r^2-(x-xc)^2}$$
$$x=x+1$$

This method of drawing a circle is inefficient because:

- 1. We are not taking advantages of the symmetry of the circle.
- 2. The amount of processing time required to perform the squaring and square root operations repeatedly.
- 3. X values are equally spaced (they differ by one unit ) the y values are not. The circle is denes and flat near the y-axis and has large gaps and is steep near the x-axis.





**H\W:** Design implicit algorithm to draw circle if the first point is at right side.

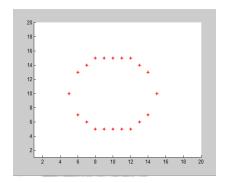
**H\W:** design implicit algorithm to draw circle if the first point is x=xc, y=yc - r

**H**\**W**: Find the point of a circle where *xc*=20, *yc*= 10 and r=8?

Example :Find the point of a circle where *xc*=10, *yc*= 10 and r=5 using direct algorithm?

Xc=10 Yc=10 X=xc-r X=10-5=5 For i=0:2\*r Y=yc+sqrt((r^2)-(x-xc)^2) Plot(x,round(y),'.y') Y=yc-sqrt((r^2)-(x-xc)^2) Plot(x,round(y),'.y') X=x+1 End

Χ	Y	Round(y)	Y	Round(y)	Plot(X,Y)
5	10	10	10	10	(5,10),(5,10)
6	13	13	7	7	(6,13),(6,7)
7	14	14	6	6	(7,14),(7,6)
8	14.5	15	5.4	5	(8,15),(8,5)
9	14.8	15	5.1	5	(9,15),(9,5)
10	15	15	5	5	(10,15),(10,5)
11	14.8	15	5.1	5	(11,15),(11,5)
12	14.5	15	5.4	5	(12,15),(12,5)
13	14	14	6	6	(13,14),(13,6)
14	13	13	7	7	(14,13),(14,7)
15	10	10	10	10	(15,10),(15,10)



## 2. parametric (polar) algorithm

One method of eliminating the problem of plotting points evenly spaced around the circle is to use polar representation of a circle:

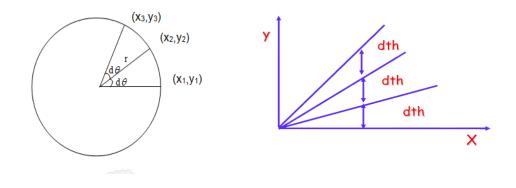
 $x = x_c + r \cos \theta$ ,

 $y = y_c + r \sin \theta$ .

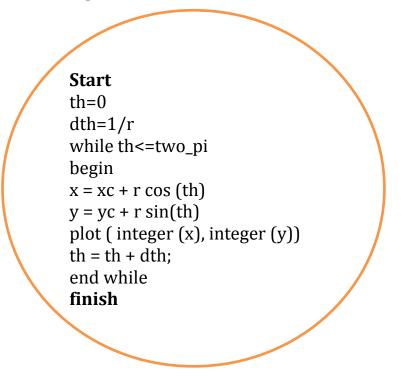
Where:  $\theta \rightarrow$  is measured in radians from 0 to 2  $\pi$ 

arc length=  $r \times \theta$ , r=radius (constant)

in this method we depend on angles to draw the circle, since it propose the first angle th=0, and end angle is two\_pi (360). The change in angle (dth) must be small value dth=1/r.



Polar algorithm



note: the algorithm use cos & sin operation and do not take the advantage of symmetric in circle

H\W: write Matlab program to draw circle using polar algorithm?

Example :Find the point of a circle where *xc*=10, *yc*= 10 and r=5 using polar algorithm ?

Th=0  
Dth=
$$1/r=1/5$$
  
While th <=2\*pi  
X=xc+r\*cos(th)  
Y=yc+r\*sin(th)  
Plot(round(x),round(y),'.k')  
Th=th+dth

End

X	Round(x)	Y	Round(y)	Th	plot(x,y)
15	15	10	10	0.2	(15,10)
14.9	15	10.9	11	0.4	(15,11)
14.6	15	11.9	12	0.6	(15,12)
14.1	14	12.8	13	0.8	(14,13)
13.4	13	13.5	14	1	(13,14)
12.7	13	14.2	14	1.2	(13,14)
11.8	12	14.6	15	1.4	(12,15)
:	:	•••	:	•	:
:	:		:		:
14.9	15	9.5	10	6.4	(15,10)

