Computer Graphics
Third stage

2018-2019

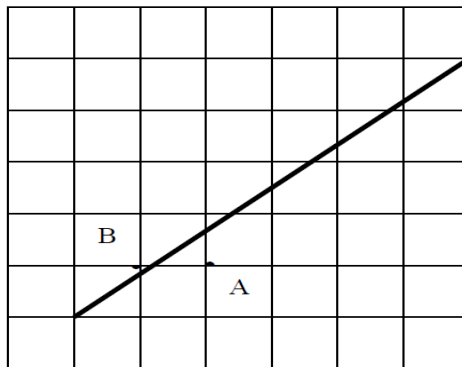Mustansiriyah university
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Arbitrary Lines

Drawing lines with arbitrary slope creates several problems, such as:

1- The display screen can be illuminated only at pixels locations; therefore a raster scan display has a staircase effect that only approximates the actual line as shown in figure below:

Although it may not be possible to choose pixels that lie on the actual line, we want to turn on pixels lying closest to it. For example, in previous figure, the pixel at location B is a better choice than the one at location A.

2- Determining the closest (best) pixels is not easy.

Different algorithms calculate different pixels to make up the approximating line.

The choice of algorithm depends on:
1- The speed of line generation.
2- The appearance of the line.
Therefore, to understand these criteria better let's look at several different line generating algorithms.

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1- Direct method:

In this method, we learn how to draw a line between two points by drawing a group of pixels using the command plot (x , y , color), with substituting in straight line equation:

$$Y = m \times X + b$$

Where (m) is the slope and (b) is a constant which represents the clipping from y-axis (y-intercept).

$$m = \frac{yend - ystart}{xend - xstart}$$, b=ystart – m * xstart

Note: start may be 1, and end may be 2.

Direct method for drawing lines can be shown in algorithm (4).

Algorithm (4):
Input: Xstart,Ystart, Xend, Yend.
Output: Arbitrary line.
```
{
   dx=Xend-Xstart
   dy=Yend-Ystart
       m=dy/dx

   b= Ystart – m * Xstart ;
   for x= Xstart to Xend  step sign(dx)
   {
    y=m *x + b;
    plot (x , y , color);
   }
}
```

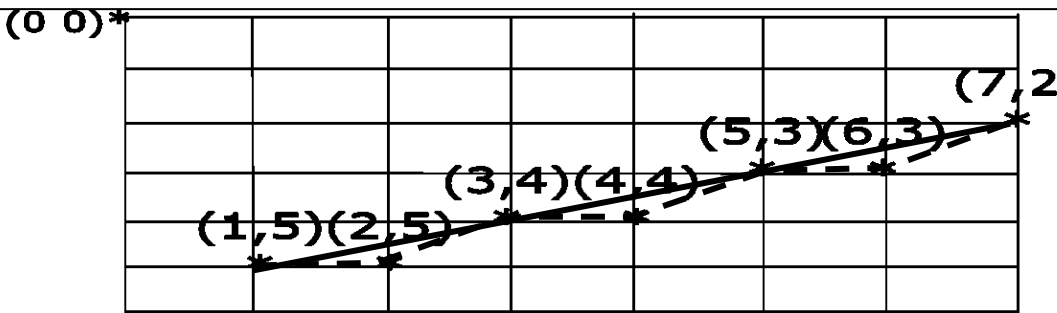Direct method is clarified in algorithm (4), assuming that:
1- Sign is a function returns (-1,0,+1) as it's argument is (<0,=0,>0).

H.W.: Write complete program in order to draw arbitrary line using direct method?

Example: trace the line where the endpoints are (1, 5), (7, 2) by Direct method , and draw the line in screen coordinate.

dx=7-1=**6**; **dy**=2-5= **-3**; **m**= -3/6= -1/2 =**-0.5**; **b**=5- (-0.5)*1=**5.5**

X	Y	Point (x, y)	Plot in screen
1	1*-0.5+5.5	(1,5)	(1,5)
2	2*-0.5+5.5	(2,4.5)	(2,5)
3	3*-0.5+5.5	(3,4)	(3,4)
4	4*-0.5+5.5	(4,3.5)	(4,4)
5	5*-0.5+5.5	(5,3)	(5,3)
6	6*-0.5+5.5	(6,2.5)	(6,3)
7	7*-0.5+5.5	(7,2)	(7,2)

H.W/ 1. Tracing same example but endpoints (7, 2) (1, 5).

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2. Simple DDA (Digital Differential Analysis)

One technique for obtaining a straight line is to solve the differential equation for straight line.

DDA Algorithm(5):

Consider one point of the line as (X1,Y1) and the second point of the line as (X2,Y2).

1. calculate dx , dy
   dx = (X2 – X1);
   dy = (Y2 – Y1);

2. Depending upon absolute value of dx & dy
   choose number of (length) to put pixel as
   length = abs(dx) if abs(dx) > abs(dy)
     Else
   length = abs(dy) if abs(dy) > abs(dx)

3. calculate increment in x & y for each steps
   Xinc = dx / length;
   Yinc = dy / length;

4. Put pixel for each step
   X = X1;
   Y = Y1;
   for (int i = 0; i <= length; i++)
   {
     plot (X,Y,'b');
     X += Xinc;
     Y += Yinc;
   }

H.W.: Write complete program in order to draw arbitrary line using DDA algorithm?

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Algorithm (5):

Input: x1,x2,y1,y2.

     i=0;

Output: Arbitrary line

{   If $(abs(x_2-x_1) \geq abs(y_2-y_1))$

       length= $abs(x_2-x_1)$;

   else

       length= $abs(y_2-y_1)$;

   dx=(x2-x1)/length;

   dy=(y2-y1)/length;

   x=x_1;

   y=y_1;

   while $(i \leq length)$

    {

      plot(round(x),round(y),color);

      x=x+ dx ;

      y=y+ dy;

      i=i+1;

}

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A simple algorithm for DDA is clarified in algorithm (5), assuming that:

1- Round is a function approximates float (real) numbers to nearest larger number.

Ex/: **trace the line where the end points between (23,33), (29,40) by DDA method.**
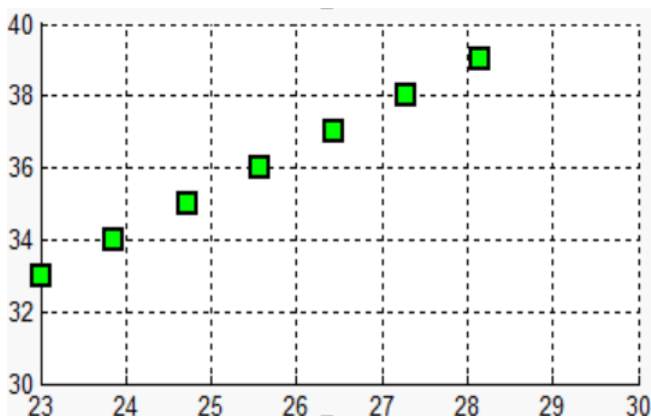
Sol/: dx=29-23=6
dy=40-33=7
Length=7
Xinc=6/7 =0.857
Yinc=7/7=1.

i	*X*	*Y*	*Plot (X)*	*Plot (y)*
0	*23*	*33*	*23*	*33*
1	*23.857*	*34*	*24*	*34*
2	*24.714*	*35*	*25*	*35*
3	*25.571*	*36*	*26*	*36*
4	*26.429*	*37*	*26*	*37*
5	*27.286*	*38*	*27*	*38*
6	*28.143*	*39*	*28*	*39*
7	*29*	*40*	*29*	*40*

NOTE:

The DDA algorithm is faster than the direct use of the line equation since it calculates points on the line without any floating point multiplication. However, a floating point addition is still needed in determining each successive point. Furthermore, cumulative error due to limited precision in the floating point representation may cause calculated points to drift away from their true position when the line relatively long.

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3.Bresenham's algorithm

- Developed by Bresenham J.E.
- Designed so that each iteration changes one of the coordinates values by ± 1.
- The other coordinate may or may not change depending on the value of an error term maintained by the algorithm.
- The error term records the distance measured perpendicular to the axis of greatest movement between the exact path of the line and the actual dots generated.

Bresenham's line algorithm is shown in algorithm (6).

Algorithm (6):

```
Input: x1,x2,y1,y2.
Output: Arbitrary line
{  x=x1 ;y=y1; dx=x2-x1; dy=y2-y1;
    e=dy/dx-0.5 ;
    for i=0 to abs(dx)
      { plot (x,y,color);
        While (e>=0)
            {
              if y1>y2
                 { y=y-1;e=e-1;
               else
                  y=y+1; e=e-1;
                 }
            }
        If x1>x2
          { x=x-1;
        else
            x=x+1;
          }
      e=e+dy/dx

      }

}
```

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H.W.: Write complete program in order to draw arbitrary line using Bresenham's algorithm?

Ex. / trace the line where the end points (50, 65), (59, 68) by Bresenham's algorithm.

Sol. / dx= 59-50= 9

dy= 68-65= 3

m= dy/dx =3/9 = 0.333

e=0.333 – 0.5 = -0.167

i	X	Y	e	
0	50	65	-0.167	+m
1	51	65	0.166	-1+m
2	52	66	-0.501	+m
3	53	66	-0.168	+m
4	54	66	0.165	-1+m
5	55	67	-0.502	+m
6	56	67	-0.169	+m
7	57	67	0.164	-1+m
8	58	68	-0.503	+m
9	59	68	-0.17	