

Theorem 1.52 (3rd Isomorphism Theorem)

$$\begin{array}{ccc} R/I & \left\{ \begin{array}{c} R \xrightarrow{\omega} R/I \\ J \xrightarrow{\omega} J/I \end{array} \right. & \{R/I\} / \{J/I\} \\ & \left[\begin{array}{c} J_1 \\ I \\ \{0\} \end{array} \right] & \left[\begin{array}{c} J_1/I \\ I/I \end{array} \right] \end{array}$$