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(b) Calculate t for the B calculated in part (a), from the monthly compounded interest formula, Equation (1).

(c) Determine the number of years and months that correspond to t.

The problem is solved by writing the following program in a script file:

When the script file is executed, the following (the values of the variables B, t, years, and months) is displayed in the Command Window:

## 1.10 PROBLEMS

The following problems can be solved by writing commands in the Command Window, or by writing a program in a script file and then executing the file.

1. Calculate:

(a) 
$$\frac{22+5.1^2}{50-6.3^2}$$

(b) 
$$\frac{44}{7} + \frac{8^2}{5} - \frac{99}{3.9^2}$$

2. Calculate:

(a) 
$$\frac{\sqrt{41^2-5.2^2}}{e^5-100.53}$$

(b) 
$$\sqrt[3]{132} + \frac{\ln(500)}{8}$$

3. Calculate:

(a) 
$$\frac{14.8^3 - 6.3^2}{(\sqrt{13} + 5)^2}$$

(b) 
$$45\left(\frac{288}{9.3}-4.6^2\right)-1065e^{-1.5}$$

4. Calculate:

(a) 
$$\frac{24.5 + 64/3.5^2 + 8.3 \cdot 12.5^2}{\sqrt{76.4} - 28/15}$$

(a) 
$$\frac{24.5 + 64/3.5^2 + 8.3 \cdot 12.5^3}{\sqrt{76.4} - 28/15}$$
 (b)  $(5.9^2 - 2.4^2)/3 + \left(\frac{\log_{10} 12890}{e^{0.3}}\right)^2$ 

5. Calculate:

(a) 
$$\cos\left(\frac{7\pi}{9}\right) + \tan\left(\frac{7}{15}\pi\right)\sin(15^\circ)$$

(a) 
$$\cos\left(\frac{7\pi}{9}\right) + \tan\left(\frac{7}{15}\pi\right)\sin(15^\circ)$$
 (b)  $\sin^2 80^\circ - \frac{(\cos 14^\circ \sin 80^\circ)^2}{\sqrt[3]{0.18}}$ 

6. Define the variable x as x = 6.7, then evaluate:

(a) 
$$0.01x^5 - 1.4x^3 + 80x + 16.7$$

(b) 
$$\sqrt{x^3 + e^x - 51/x}$$

7. Define the variable t as t = 3.2, then evaluate:

(a) 
$$56t - 9.81\frac{t^2}{2}$$

(b) 
$$14e^{-0.1t}\sin(2\pi t)$$

8. Define the variables x and y as x = 5.1 and y = 4.2, then evaluate:

(a) 
$$\frac{3}{4}xy - \frac{7x}{v^2} + \sqrt{xy}$$

(b) 
$$(xy)^2 - \frac{x+y}{(x-y)|^2} + \sqrt{\frac{x+y}{2x-y}}$$

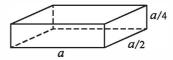
9. Define the variables a, b, c, and d as:

$$a = 12$$
,  $b = 5.6$ ,  $c = \frac{3a}{b^2}$ , and  $d = \frac{(a-b)^c}{c}$ , then evaluate:

(a) 
$$\frac{a}{b} + \frac{d-c}{d+c} - (d-b)^2$$

(b) 
$$e^{\frac{d-c}{a-2b}} + \ln\left(\left|c-d+\frac{b}{a}\right|\right)$$

10. A sphere has a radius of 24 cm. A rectangular prism has sides of a, a/2, and a/4.

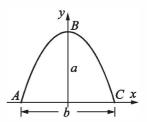


- (a) Determine a of a prism that has the same volume as the sphere.
- (b) Determine a of a prism that has the same surface area as the sphere.

11. The arc length of a segment of a parabola ABC of an ellipse with semi-minor axes a and b is given approximately by:

$$L_{ABC} = \frac{1}{2} \sqrt{b^2 + 16a^2} + \frac{b^2}{8a} \ln \left( \frac{4a + \sqrt{b^2 + 16a^2}}{b} \right) \, .$$

(a) Determine  $L_{ABC}$  if a = 11 in. and b = 9 in.



12. Two trigonometric identities are given by:

(a) 
$$\sin 5x = 5\sin x - 20\sin^3 x + 16\sin^5 x$$
 (b)  $\sin^2 x \cos^2 x = \frac{1 - \cos 4x}{8}$ 

For each part, verify that the identity is correct by calculating the values of the left and right sides of the equation, substituting  $x = \frac{\pi}{12}$ .

13. Two trigonometric identities are given by:

(a) 
$$\tan 3x = \frac{3\tan x - \tan^3 x}{1 - 3\tan^2 x}$$

(b) 
$$\cos 4x = 8(\cos^4 x - \cos^2 x) + 1$$

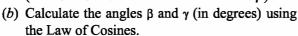
For each part, verify that the identity is correct by calculating the values of the left and right sides of the equation, substituting  $x = 24^{\circ}$ .

14. Define two variables:  $alpha = \pi/6$ , and  $beta = 3\pi/8$ . Using these variables, show that the following trigonometric identity is correct by calculating the values of the left and right sides of the equation.

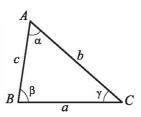
$$\sin\alpha + \sin\beta = 2\sin\left(\frac{\alpha+\beta}{2}\right)\cos\left(\frac{\alpha-\beta}{2}\right)$$

- 15. Given:  $\int x \sin ax dx = \frac{\sin ax}{a^2} \frac{x \cos ax}{a}$ . Use MATLAB to calculate the following definite integral:  $\int_{\frac{\pi}{3}}^{\frac{3\pi}{2}} x \sin(0.6x) dx$ .
- 16. In the triangle shown a = 5.3 in.,  $\gamma = 42^{\circ}$ , and b = 6 in. Define a,  $\gamma$ , and b as variables, and then:
  - (a) Calculate the length b by using the Law of Cosines.

(Law of Cosines:  $c^2 = a^2 + b^2 - 2ab\cos\gamma$ )



(c) Check that the sum of the angles is 180°.

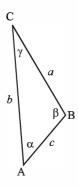


- 17. In the triangle shown a = 5 in., b = 7 in., and  $\gamma = 25^{\circ}$ . Define a, b, and  $\gamma$  as variables, and then:
  - (a) Calculate the length of c by substituting the variables in the Law of Cosines.

(Law of Cosines:  $c^2 = a^2 + b^2 - 2ab\cos\gamma$ )

- (b) Calculate the angles  $\alpha$  and  $\beta$  (in degrees) using the Law of Sines.
- (c) Verify the Law of Tangents by substituting the results from part (b) into the right and left sides of the equation.

Law of Tangents: 
$$\frac{a-b}{a+b} = \frac{\tan\left[\frac{1}{2}(\alpha-\beta)\right]}{\left[\frac{1}{2}(\alpha+\beta)\right]}$$

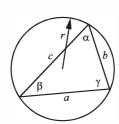


- 18. In the ice cream cone shown, L=4 in. and  $\theta=35^{\circ}$ . The cone is filled with ice cream such that the portion above the cone is a hemisphere. Determine the volume of the ice cream.
- 19. For the triangle shown, a = 48 mm, b = 34 mm, and  $\gamma = 83^{\circ}$ . Define a, b, and  $\gamma$  as variables, and then:
  - (a) Calculate c by substituting the variables in the Law of Cosines.

(Law of Cosines: 
$$c^2 = a^2 + b^2 - 2ab\cos\gamma$$
)

(b) Calculate the radius r of the circle circumscribing the triangle using the formula:

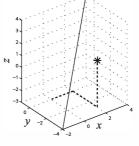
$$r = \frac{abc}{4\sqrt{s(s-a)(s-b)(s-c)}}$$
where  $s = (a+b+c)/2$ .



20. The parametric equations of a line in space are:  $x = x_0 + at$ ,  $y = y_0 + bt$ , and  $z = z_0 + ct$ . The distance d from a point  $A(x_A, y_A, z_A)$  to the line can be calculated by:

$$d = d_{A0} \sin \left[ a \cos \left( \frac{(x_A - x_0)a + (y_A - y_0)b + (z_A - z_0)c}{d_{A0} \sqrt{a^2 + b^2 + c^2}} \right) \right]$$

where 
$$d_{A0} = \sqrt{(x_A - x_0)^2 + (y_A - y_0)^2 + (z_A - z_0)^2}$$
. Determine the distance of the point  $A$  (2, -3, 1)



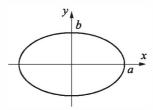
from the line x = -4 + 0.6t, y = -2 + 0.5t, and z = -3 + 0.7t. First define the variables  $x_0$ ,  $y_0$ ,  $z_0$ , a, b, and c, then use the variable (and the coordinates of point A) to calculate the variable  $d_{A0}$ , and finally calculate d.

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21. The circumference of an ellipse can be approximated by:

$$C = \pi[3(a+b) - \sqrt{(3a+b)(a+3b)}]$$

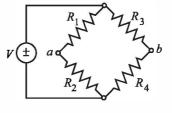
Calculate the circumference of an ellipse with a = 16 in. and b = 11 in.



- 22. 315 people have to be transported using buses that have 37 seats. By typing one line (command) in the Command Window, calculate how many seats will remain empty if enough buses will be ordered to transport all the people. (Hint: use MATLAB built-in function ceil.)
- 23. 739 apples are to be packed and shipped such that 54 are placed in a box. By typing one line (command) in the Command Window, calculate how many apples will remain unpacked if only full boxes can be shipped. (Hint: use MATLAB built-in function fix.)
- 24. Assign the number 316,501.673 to a variable, and then calculate the following by typing one command:
  - (a) Round the number to the nearest hundredth.
  - (b) Round the number to the nearest thousand.
- 25. The voltage difference  $V_{ab}$  between points a and b in the Wheatstone bridge circuit is:

$$V_{ab} = V \left( \frac{R_1 R_3 - R_2 R_4}{(R_1 + R_2)(R_3 + R_4)} \right)$$

Calculate the voltage difference when V = 14 volts,  $R_1 = 120.6$  ohms,  $R_2 = 119.3$  ohms,  $R_3 = 121.2$  ohms, and  $R_4 = 118.8$  ohms.



26. The resonant frequency f (in Hz) for the circuit shown is given by:

$$f = \frac{1}{2\pi} \sqrt{\frac{1}{LC} - \left(\frac{R}{L}\right)^2}$$

Calculate the resonant frequency when  $L=0.15\,\mathrm{hen}$ -rys,  $R=14\,\mathrm{ohms}$ , and  $C=2.6\times10^{-6}\,\mathrm{farads}$ .

