## Example 2



## Solution:

Step 1: Develop a phase plan, each left turn movement should be checked against the criteria

EB: $\mathrm{V}_{\mathrm{LT}}=35<200$

$$
\text { Xprod }=35 *\left(\frac{500}{2}\right)=8750<50000
$$

So, no protection needed.
WB: $\mathrm{V}_{\mathrm{LT}}=25<200$

$$
\text { Xprod }=25 *\left(\frac{600}{2}\right)=22875<50000
$$

So, no protection needed.
NB: $\mathrm{V}_{\mathrm{LT}}=250>200$
So, protection needed.
SB: $\mathrm{V}_{\mathrm{LT}}=220>200$
So, protection needed.

Based on the above;
The NB and SB left turns require a protected phase, so an exclusive left turn phase will be used on the N-S arterial. A signal phase using permitted left turns will be used on the E-W arterial.

## Phase A



Phase B


Phase C


Step 2: Convert volumes to through vehicle equivalent

| Approach | Movement | Volume(veh/hr) | Equivalent | Volume <br> (veh/hr) | Lane group <br> volume <br> (tvu/h) | Vol/lane <br> (tvu/hr/ln) |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| EB | L | 35 | 4.00 | 140 | 140 | 140 |
|  | T | 610 | 1.00 | 610 | 702 | 351 |
| R | 70 | 1.32 | 92 |  | 128 |  |

Traffic Engineering
Solved Examples
Prof. Dr. Zainab Akaissi

|  | T | 500 | 1.00 | 500 | 566 | 283 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| NB | R | 50 | 1.32 | 66 |  |  |
|  | L | 220 | 1.05 | 231 | 231 | 231 |
|  | T | 700 | 1.00 | 700 | 944 | 472 |
| SB | L | 185 | 1.32 | 244 |  |  |
|  | T | 250 | 1.05 | 263 | 263 | 263 |
|  | R | 175 | 1.00 | 800 | 1031 | 516 |

Step 3: Determine the critical lane volumes

|  | Ring 1 | Ring 2 | Critical Volume |  |
| :--- | :--- | :--- | :--- | :--- |
| Phase A |  |  |  | 231 or 263 <br> $\mathrm{~V}_{\mathrm{cA}}=263 \mathrm{tuv} / \mathrm{hr}$ |
| Phase B |  |  |  | 472 or 516 <br> $\mathrm{~V}_{\mathrm{cB}}=516 \mathrm{tvu} / \mathrm{hr}$ |
| Phase C |  |  |  |  |

Total critical volume $\mathrm{V}_{\mathrm{c}}=263+516+351=1130 \mathrm{tvu} / \mathrm{hr}$

## Step 4: Determine Yellow and All -Red Intervals

$Y_{A, B, C}=1.0+\frac{1.47 \times 45}{(2 \times 10)+(0)}=4.3 \mathrm{sec}$.
The width of the $\mathrm{N}-\mathrm{S}$ street is 55 ft , and the width of the E-W street is 60 ft .
The width of a crosswalk is 10 ft . During the N-S left turn phase, it will be assumed that a vehicle must clear the entire width of the E-W artery.

Thus, for phase A, the width to be cleared (P) is: $60+10=70 \mathrm{ft}$.
For phase B, it is also $60+10=70 \mathrm{ft}$.
For phase C, the distance to be cleared is $55+10=65 \mathrm{ft}$
Thus,
$\operatorname{ar}_{\mathrm{A}, \mathrm{B}}=\frac{70+20}{1.47 * 45}=1.4 \mathrm{sec}$.
$\operatorname{ar}_{\mathrm{C}}=\frac{65+20}{1.47 * 45}=1.3 \mathrm{sec}$.
Where 20 ft is assumed length of a typical vehicle.

Step 5: Determine the lost times
The lost time $l_{2}$ and e are both default values of 2 sec .
$\mathrm{Y}_{\mathrm{A}, \mathrm{B}}=\mathrm{t}_{\mathrm{LA}, \mathrm{B}}=4.3+1.4=5.7 \mathrm{sec}$.
$\mathrm{Y}_{\mathrm{C}}=\mathrm{t}_{\mathrm{C}}=4.3+1.3=5.6 \mathrm{sec}$.
Based on this, the total lost time per cycle, $\mathrm{L}=5.7+5.7+5.6=17.0 \mathrm{sec}$.
Noting $\mathrm{Y}_{\mathrm{A}, \mathrm{B}}$ occurs twice, at the end both phases A and C.

Step 6: Determine the desirable cycle length
The desirable cycle length is found using equation below:

$$
C_{d e s}=\frac{17}{1-\left(\frac{1130}{1615 * 0.92 * 0.9}\right)}=109.7 \mathrm{sec} .
$$

A cycle length of 110 sec . would be selected.

## Step 7: Allocate effective green to each phase

In a cycle length of 110 sec . with 17 sec . of lost time per cycle, amount of effective green that must be allocated to the three phases is $110-17=93 \mathrm{sec}$.

The effective green time is allocated in proportion to the phase critical -lane volumes:

Thus; $\mathrm{g}_{\mathrm{A}}=93 \times\left(\frac{263}{1130}\right)=21.6 \mathrm{sec}$.
$g_{B}=93 \times\left(\frac{516}{1130}\right)=42.5 \mathrm{sec}$.
$g_{C}=93 \times\left(\frac{351}{1130}\right)=28.9 \mathrm{sec}$.
The cycle length is now checked to ensure that the sum of all effective green times and the lost time equal 110 sec .
$21.6+42.5+28.9+17.0=110$ OK
Note that when default values for $1_{1}$ and e (both 2 sec .) are used, actual green times, G , equal effective green, g .
$\mathrm{G}_{\mathrm{A}}=21.6 \mathrm{sec}$.
$\mathrm{G}_{\mathrm{B}}=42.5 \mathrm{sec}$.
$\mathrm{G}_{\mathrm{C}}=28.9 \mathrm{sec}$.

## Step 8: Check for pedestrian requirements

Note the pedestrians will be permitted to cross the E-W artery only during phase B. Pedestrian will cross the N-S artery during phase C . The number of pedestrians per
cycle for all crosswalks is the default pedestrian volume for moderate activity, 200 peds/hr, divided by the number of cycles in an hour ( $3600 / 110=32.7$ cycles $/ \mathrm{hr}$ ). Thus $\mathrm{N}_{\text {ped }}=200 / 32.7=6.1$ peds/cycle. Required pedestrian green times are:
$\mathrm{G}_{\mathrm{pB}}=3.2+(0.27 * 6.1)+(60 / 4.0)=48>2 \mathrm{sec} . \mathrm{ok}$
$\mathrm{G}_{\mathrm{pC}}=3.2+(0.27 * 6.1)+(55 / 4.0)=34.5 \mathrm{sec} . \mathrm{ok}$
The minimum requirements are compared to the sum of the green, yellow, and all red times provided for vehicles:
$\mathrm{G}_{\mathrm{pB}}=19.8 \mathrm{sec} .<\mathrm{G}_{\mathrm{B}}+\mathrm{Y}_{\mathrm{B}}=42.5+5.7=48.2 \mathrm{sec} . \mathrm{ok}$
$\mathrm{G}_{\mathrm{pC}}=18.6 \mathrm{sec} .<\mathrm{G}_{\mathrm{C}}+\mathrm{Y}_{\mathrm{C}}=28.9+5.6=34.5 \mathrm{sec} . \mathrm{ok}$
Therefore no changes on signal timing are required to accommodate pedestrians safely.

For major arterials crossing, pedestrian signal would normally be provided. During phase A, all pedestrian signals would indicate "DON T WALK". During phase B, the pedestrian clearance interval (the flashing DON T WALK) would be $\mathrm{LSS}_{\mathrm{p}}$ or $60 \backslash 4.0=15.0 \mathrm{sec}$.

The WALK interval is whatever time is left in G+Y, (or G+y, or G) counting from the end of Y (or y or G): using G+Y, 48.2-15.0 $=33.2 \mathrm{sec}$.

During phase C, $\mathrm{L} / \mathrm{S}_{\mathrm{p}}$ is $55 \backslash 4.0=13.8 \mathrm{sec}$., and the WALK interval would be $34.5-$ $13.8=20.7 \mathrm{sec}$.

## Example 3



## Solution:

Step 1: Develop a phase plan, each left turn movement should be checked against the criteria

EB: $\mathrm{V}_{\mathrm{LT}}=300>200 \mathrm{veh} / \mathrm{hr}$
So, protection needed.
WB: $\mathrm{V}_{\mathrm{LT}}=150<200 \mathrm{veh} / \mathrm{hr}$

$$
\text { Xprod }=150 *\left(\frac{1200}{3}\right)=60000>50000
$$

So, protection needed.
$\mathrm{NB}: \mathrm{V}_{\mathrm{LT}}=50<200 \mathrm{veh} / \mathrm{hr}$
Xprod $=50 *\left(\frac{400}{2}\right)=10000<50000$
So, protection are not needed.
SB: $\mathrm{V}_{\mathrm{LT}}=30<200$

Xprod $=30 *\left(\frac{500}{2}\right)=7500<50000$
So, protection are not needed.

Based on the above;
The E-W approaches have LT lanes, and protected left turns are needed on both approaches. Because the LT volumes EB and WB are very different ( $300 \mathrm{veh} / \mathrm{hr}$ versus $150 \mathrm{veh} / \mathrm{hr}$ ), a phase plan that splits the protected LT phases would be advisable. An exclusive LT phase followed by a leading green for the EB direction, will be employed for E-W artery.


Step 2: Convert volumes to through vehicle equivalent

| Approach | Movement | Volume(veh/hr) | Equivalent | Volume <br> (veh/hr) | Lane group <br> volume <br> (tvu/h) | Vol/lane <br> $(\mathbf{t v u} / \mathbf{h r} / \mathbf{l n})$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| EB | L | 300 | 1.05 | 315 | 315 | 315 |
|  | T | 1200 | 1.00 | 1200 | 1200 | 400 |
| WB | L | 100 | 1.18 | 118 | 118 | 118 |
|  | T | 150 | 1.05 | 158 | 158 | 158 |
|  | R | 1000 | 1.00 | 1000 | 1000 | 334 |
| NB | L | 50 | 1.18 | 295 | 295 | 295 |
|  | T | 500 | 3.00 | 150 |  |  |
|  | R | 40 | 1.00 | 500 | 697 | 349 |
| SB | L | 30 | 4.18 | 47 |  |  |
|  | T | 400 | 1.00 | 400 | 591 | 296 |
|  | R | 60 | 1.18 | 71 |  |  |

Step 3: Determine the critical lane volumes

|  | Ring 1 | Ring 2 | Critical Volume |
| :---: | :---: | :---: | :---: |
| Phase A1 |  | $158$ | $\begin{aligned} & 315+334=649 \\ & \text { Or } \end{aligned}$ |
| Phase A2 |  | 400 | $158+400=558$ |
| Phase A3 | $\begin{gathered} 295 \\ 334 \\ \qquad \begin{array}{c} 29 \\ \leftarrow \end{array} \end{gathered}$ | $118$ | $\mathrm{V}_{\mathrm{cA}}=649 \mathrm{tvu} / \mathrm{hr}$ |
| Phase B |  |  | 296 or 349 <br> $\mathrm{V}_{\mathrm{cB}}=349 \mathrm{tvu} / \mathrm{hr}$ |

Total critical volume $\mathrm{V}_{\mathrm{c}}=649+349=998 \mathrm{tvu} / \mathrm{hr}$

Step 4: Determine Yellow and All -Red Intervals

Percentile speeds are estimated from the measured average speeds given:
$\mathrm{S}_{8 \mathrm{SEW}}=50+5=55 \mathrm{mile} / \mathrm{hr}$
$\mathrm{S}_{15 \mathrm{EW}}=50-5=45 \mathrm{mile} / \mathrm{hr}$
$\mathrm{S}_{85 \mathrm{NS}}=35+5=40 \mathrm{mile} / \mathrm{hr}$
$\mathrm{S}_{15 \mathrm{NS}}=35-5=30 \mathrm{mile} / \mathrm{hr}$

Then:
$\mathrm{Y}_{\mathrm{A} 1, \mathrm{~A} 2, \mathrm{~A} 3}=1.0+\frac{1.47 \times 55}{(2 \times 10)+(0)}=5.0 \mathrm{sec}$.
$Y_{B}=1.0+\frac{1.47 \times 40}{(2 \times 10)+(0)}=3.9 \mathrm{sec}$.
$\operatorname{ar}_{\mathrm{A} 1, \mathrm{~A} 2, \mathrm{~A} 3}=\frac{40+20}{1.47 * 45}=0.9 \mathrm{sec}$.
$\operatorname{ar}_{B}=\frac{96+20}{1.47 * 30}=2.6 \mathrm{sec}$.

Where 20ft is assumed length of a typical vehicle.

Step 5: Determine the lost times
Because the problem statement specifies the default values of 2.0 sec . each for startup lost time and extension of effective green into yellow and all-red intervals, the total lost time in each phase, $\mathrm{t}_{\mathrm{L}}$ is equal to the sum of the yellow and all -red intervals, Y. Thus:
$\mathrm{t}_{\mathrm{LA} 1 / \mathrm{A} 2}=\mathrm{Y}_{\mathrm{A} 1 / \mathrm{A} 2}=5.0+0.9=5 \mathrm{sec}$.
$\mathrm{t}_{\mathrm{LA} 3}=\mathrm{Y}_{\mathrm{A} 3}=5.0+0.9=5.9 \mathrm{sec}$.
$\mathrm{t}_{\mathrm{LB}}=\mathrm{Y}_{\mathrm{B}}=3.9+2.6=6.5 \mathrm{sec}$.
Total lost time per cycle,
$\mathrm{L}=5.9+5.9+6.5=18.3 \mathrm{sec}$.
Step 6: Determine the desirable cycle length
The desirable cycle length is found using equation below:

$$
C_{\text {des }}=\frac{18.3}{1-\left(\frac{998}{1615 * 0.85 * 0.9}\right)}=95.3 \mathrm{sec} .
$$

A cycle length of 100 sec . would be selected.

Step 7: Allocate effective green to each phase
In a cycle length of 100 sec . with 18.3 sec . of lost time per cycle, amount of effective green that must be allocated to the phases is $100-18.3=81.7 \mathrm{sec}$.

Note that in allocating green to the critical path, phases A1 and phase A2 are treated as a single segment.
$\mathrm{g}_{\mathrm{A} 1+\mathrm{A} 2}=81.7 *\left(\frac{315}{998}\right)=25.8 \mathrm{sec}$.
$\mathrm{g}_{\mathrm{A} 3}=81.7 *\left(\frac{334}{998}\right)=27.3 \mathrm{sec}$.
$\mathrm{g}_{\mathrm{B}}=81.7 *\left(\frac{349}{998}\right)=28.6 \mathrm{sec}$.
The specific lengths of phases A1 and A2 are determined by fixing the ring 2 transition between them. This requires consideration of non-critical path through combined phase A, which occurs on ring 2. The total length of combined Phase A is the sum of $g_{A 1+A 2}$ and $g_{A 3}$ :
$25.8+27.3=53.1 \mathrm{sec}$.
The ring 2 transition is based on the relative values of the lane volumes for phase A1 and the combined phase A2/A3, or:
$\mathrm{g}_{\mathrm{Al}}=53.1 *\left(\frac{158}{158+400}\right)=15.0 \mathrm{sec}$.
By implication, phase A2 is the total length of combined phase A minus the length of phase A1 and phase A3:
$\mathrm{g}_{\mathrm{A} 2}=53 \cdot 1-15 \cdot 0-27.3=10.8 \mathrm{sec}$.

With the assumption of default values for $l_{2}(2.0 \mathrm{sec}$.$) and \mathrm{e}=2.0 \mathrm{sec}$., actual green times are equal to effective green times (numerically, although they do not occur simultaneously):
$\mathrm{G}_{\mathrm{Al}}=15.0 \mathrm{sec}$.
$\mathrm{G}_{\mathrm{A} 2}=10.8 \mathrm{sec}$.
$\mathrm{Y}_{\mathrm{A} 1 / \mathrm{A} 2}=5.9 \mathrm{sec}$.
$\mathrm{G}_{\mathrm{A} 3}=27.3 \mathrm{sec}$.
$\mathrm{Y}_{\mathrm{A} 3}=5.9 \mathrm{sec}$.
$\mathrm{G}_{\mathrm{B}}=28.6 \mathrm{sec}$.
$Y_{B}=6.5 \mathrm{sec}$.
$\mathrm{C}=100.0 \mathrm{sec}$.

There is no step 8 in this example because there are no pedestrians at this intersection and therefore, no pedestrian requirements to be checked.

## Example 4



## Solution:

Step 1: Develop a phase plan, each left turn movement should be checked against the criteria

WB: $\mathrm{V}_{\mathrm{LT}}=300>200 \mathrm{veh} / \mathrm{hr}$
So, protection needed. There is no EB or SB left turn. And the NB left turn is unopposed. So the necessary providing phase would be to use a leading WB green with no logging EB green.

| Phase A1 |  | 700 |
| :---: | :---: | :---: |
| Phase A2 |  |  |
| Phase B | $333$ |  |

Step 2: Convert volumes to through vehicle equivalent

| Approach | Movement | Volume(veh/hr) | Equivalent | Volume <br> (veh/hr) | Lane group <br> volume <br> (tvu/h) | Vol/lane <br> $(\mathbf{t v u} / \mathbf{h r} / \mathbf{l n})$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| EB | T | 700 | 1.00 | 700 | 821 | 411 |
| WB | L | 380 | 1.21 | 121 |  |  |
|  | T | 700 | 1.05 | 399 | 399 | 399 |
|  |  | 1.00 | 700 | 700 | 700 |  |
| NB | L | 300 | 1.10 | 330 | 330 | 330 |
|  | R | 250 | 1.21 | 303 | 303 | 303 |

Step 3: Determine the critical lane volumes


Total critical volume $\mathrm{V}_{\mathrm{c}}=810+330=1140 \mathrm{tvu} / \mathrm{hr}$

Step 4: Determine Yellow and All -Red Intervals
$\mathrm{Y}_{\mathrm{A} 1, \mathrm{~A} 2, \mathrm{~B}}=1.0+\frac{1.47 \times 35}{(2 \times 10)+(0)}=3.6 \mathrm{sec}$.
Thus,
$\operatorname{ar}_{\mathrm{A} 1, \mathrm{~A} 2}=\frac{39+20}{1.47 * 35}=1.1 \mathrm{sec}$.
$\operatorname{ar}_{\mathrm{B}}=\frac{48+20}{1.47 * 35}=1.3 \mathrm{sec}$.
Where 20 ft is assumed length of a typical vehicle.

Step 5: Determine the lost times
The lost time $1_{2}$ and e are both default values of 2 sec .
$\mathrm{Y}_{\mathrm{Al}}=\mathrm{t}_{\mathrm{LA} 1}=3.6+1.1=4.7 \mathrm{sec}$.
$\mathrm{Y}_{\mathrm{A} 2}=\mathrm{t}_{\mathrm{LA} 2}=3.6+1.1=4.7 \mathrm{sec}$.
$Y_{B}=t_{L B}=3.6+1.3=4.9 \mathrm{sec}$.

Based on this, the total lost time per cycle, $\mathrm{L}=4.7+4.7+4.9=14.3 \mathrm{sec}$.

Step 6: Determine the desirable cycle length
The desirable cycle length is found using equation below:

$$
C_{d e s}=\frac{14.3}{1-\left(\frac{1140}{1615 * 0.92 * 0.95}\right)}=74.5 \mathrm{sec} .
$$

A cycle length of 75 sec . would be selected.

Step 7: Allocate effective green to each phase
In a cycle length of 75 sec . with 14.3 sec . of lost time per cycle, amount of effective green that must be allocated to the three phases is $75-14.3=60.7 \mathrm{sec}$.

The effective green time is allocated in proportion to the phase critical -lane volumes:

Thus; $\mathrm{g}_{\mathrm{Al}}=60.7 \times\left(\frac{399}{1140}\right)=21.2 \mathrm{sec}$.
$\mathrm{g}_{\mathrm{A} 2}=60.7 \times\left(\frac{411}{1140}\right)=21.9 \mathrm{sec}$.
$g_{B}=60.7 \times\left(\frac{330}{1140}\right)=17.6 \mathrm{sec}$.
Note that when default values for $l_{1}$ and e (both 2 sec .) are used, actual green times, G , equal effective green, g .
$\mathrm{G}_{\mathrm{Al}}=21.2 \mathrm{sec}$.
$\mathrm{G}_{\mathrm{A} 2}=21.9 \mathrm{sec}$.
$G_{B}=17.6$ sec.

Step 8: Check for pedestrian requirements
Although there is low pedestrian activity at this intersection, pedestrian must still be safety accommodated by signal phasing.

It will be assumed the pedestrians cross N-S Street only during phase A2 and that pedestrians crossing the E-W Street will use phase B.

The number of pedestrians per cycle for all crosswalks is the default pedestrian volume for moderate activity, 50 peds/hr, divided by the number of cycles in an hour ( $3600 / 75=48$ cycles/hr). Thus $\mathrm{N}_{\text {ped }}=50 / 48=1.0$ peds/cycle. Required pedestrian green times are:

$$
\begin{aligned}
& \mathrm{G}_{\mathrm{pA} 2}=3.2+(0.27 * 1)+(39 / 4.0)=13.2 \mathrm{sec} . \\
& \mathrm{G}_{\mathrm{pB}}=3.2+(0.27 * 1)+(48 / 4.0)=15.5 \mathrm{sec} .
\end{aligned}
$$

The minimum requirements are compared to the sum of the green, yellow, and all red times provided for vehicles:
$\mathrm{G}_{\mathrm{pA} 2}=13.2 \mathrm{sec} .<\mathrm{G}_{\mathrm{A}_{2}}+\mathrm{Y}_{\mathrm{A} 2}=21.9+4.7=26.6 \mathrm{sec} . \mathrm{ok}$
$\mathrm{G}_{\mathrm{p} B}=15.5 \mathrm{sec} .<\mathrm{G}_{\mathrm{B}}+\mathrm{Y}_{\mathrm{B}}=17.6+4.9=22.5 \mathrm{sec} . \mathrm{ok}$
Therefore no changes on signal timing are required to accommodate pedestrians safely.
It is noticed that pedestrians could be entirely accommodated by green and that it is not necessary in this case to allow pedestrians in the cross walk during the $y$ and ar interval.

