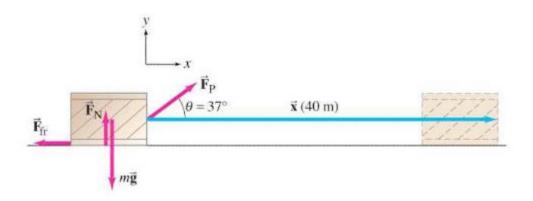
EXAMPLE 6–1 Work done on a crate. A person pulls a 50-kg crate 40 m along a horizontal floor by a constant force $F_P = 100 \text{ N}$, which acts at a 37° angle as shown in Fig. 6–3. The floor is rough and exerts a friction force $F_{fr} = 50 \text{ N}$. Determine (a) the work done by each force acting on the crate, and (b) the net work done on the crate.



SOLUTION (a) The work done by the gravitational and normal forces is zero, since they are perpendicular to the displacement \vec{x} ($\theta = 90^{\circ}$ in Eq. 6–1):

$$W_{\rm G} = mgx\cos 90^{\circ} = 0$$

$$W_{\rm N} = F_{\rm N} x \cos 90^{\circ} = 0.$$

The work done by $\vec{\mathbf{F}}_{P}$ is

$$W_P = F_P x \cos \theta = (100 \text{ N})(40 \text{ m}) \cos 37^\circ = 3200 \text{ J}.$$

The work done by the friction force is

$$W_{\rm fr} = F_{\rm fr} x \cos 180^{\circ} = (50 \,\mathrm{N})(40 \,\mathrm{m})(-1) = -2000 \,\mathrm{J}.$$

The angle between the displacement $\vec{\mathbf{x}}$ and the force $\vec{\mathbf{F}}_{fr}$ is 180° because they point in opposite directions. Since the force of friction is opposing the motion (and $\cos 180^\circ = -1$), the work done by friction on the crate is *negative*.

- (b) The net work can be calculated in two equivalent ways:
- (1) The net work done on an object is the algebraic sum of the work done by each force, since work is a scalar:

$$W_{\text{net}} = W_{\text{G}} + W_{\text{N}} + W_{\text{P}} + W_{\text{fr}}$$

= 0 + 0 + 3200 J - 2000 J
= 1200 J.

(2) The net work can also be calculated by first determining the net force on the object and then taking its component along the displacement: $(F_{\text{net}})_x = F_{\text{P}} \cos \theta - F_{\text{fr}}$. Then the net work is

$$W_{\text{net}} = (F_{\text{net}})_x x = (F_{\text{P}} \cos \theta - F_{\text{fr}}) x$$

= $(100 \text{ N} \cos 37^\circ - 50 \text{ N})(40 \text{ m})$
= 1200 J .

In the vertical (y) direction, there is no displacement and no work done.