

# Single phase Motors

2. Rotor at running

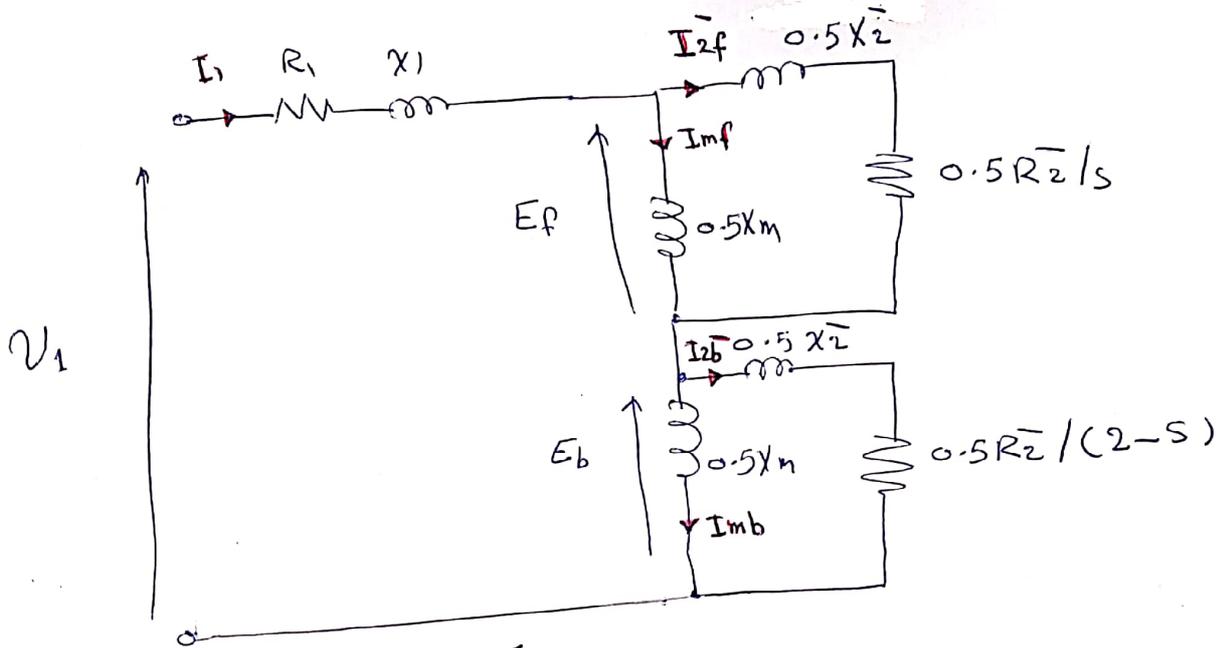
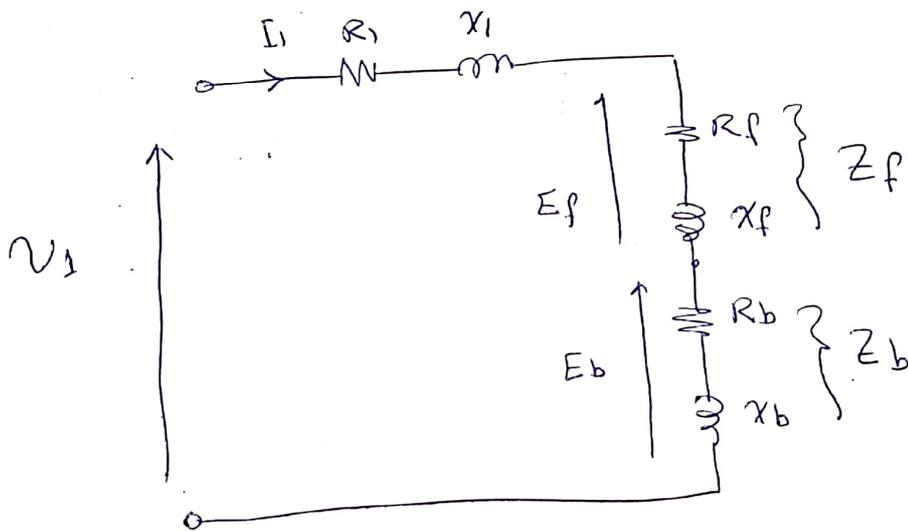


Fig. 11



$$Z_f = R_f + jX_f = j0.5X_m \parallel (0.5R_2/s + j0.5X_2)$$

$$Z_b = (R_b + jX_b) = j0.5X_m \parallel (0.5R_2/(2-s) + j0.5X_2)$$

Fig. 12

$$\text{Input power} = P_i = V_1 I_1 \cos \phi$$

$$P_i = P_{CL} + P_{sr}$$

$$P_{sr} = P_{gf} + P_{gb}$$

$$\begin{aligned} \text{Forward air gap power} &= P_{gf} = I_1^2 \frac{R_2}{s} \\ &= I_1^2 R_f \end{aligned}$$

$$\begin{aligned} \text{Backward air gap power} &= P_{gb} = I_1^2 \frac{R_2}{2-s} \\ &= I_1^2 R_b \end{aligned}$$

$$T_f = \frac{P_{gf}}{\omega_s} \quad , \quad T_b = \frac{P_{gb}}{\omega_s}$$

$$T = T_f - T_b$$

$$= \frac{1}{\omega_s} I_1^2 (R_f - R_b)$$

$$= \frac{1}{\omega_s} (P_{gf} - P_{gb})$$

$$\text{mechanical developed power} = P_m$$

$$P_m = T \cdot \omega_r \quad , \quad \omega_r = (1-s)\omega_s$$

$$\therefore P_m = T \cdot (1-s)\omega_s$$

$$= (1-s)\omega_s \cdot \frac{1}{\omega_s} (P_{gf} - P_{gb})$$

$$= (1-s)(P_{gf} - P_{gb})$$

## Single phase Motors

$$\frac{0.5 \bar{R}_2}{s} = 0.5 \bar{R}_2 + 0.5 \bar{R}_2 \frac{(1-s)}{s}$$
$$= R_{\text{cuf}} + R_{\text{mech.f}}$$

$$R_{\text{cuf}} = s \cdot \frac{0.5 \bar{R}_2}{s}, \quad R_{\text{mech.f}} = (1-s) \cdot \frac{0.5 \bar{R}_2}{s}$$

$$\frac{0.5 \bar{R}_2}{2-s} = 0.5 \bar{R}_2 + 0.5 \bar{R}_2 \frac{1-(2-s)}{2-s}$$
$$= R_{\text{cub}} + R_{\text{mech.b}}$$

forward rotor copper losses =  $P_{\text{rcuf}} = s P_{\text{gf}}$

backward rotor copper losses =  $P_{\text{rcub}} = (2-s) P_{\text{gb}}$

$$P_{\text{rcu}} = s P_{\text{gf}} + (2-s) P_{\text{gb}}$$

$$P_m = (1-s) P_{\text{gf}} + [1-(2-s)] P_{\text{gb}}$$

$$= (1-s) P_{\text{gf}} + [-1+s] P_{\text{gb}}$$

$$= (1-s) (P_{\text{gf}} - P_{\text{gb}})$$

$$P_o = P_m - P_{\text{rot}} \quad , P_o = \text{output power}$$

$P_{\text{rot}} = \text{core + frictional + windage losses}$

$$T_L = \text{load torque}$$

$$= \frac{P_o}{\omega_r}$$